



8117

## M.Sc. (Sem.-VIII) Examination, 2022-23

Booklet Series

**A****PHYSICS****Statistical Physics**

(To be filled in by the Candidate / निम्न पूर्तियों परीक्षार्थी स्वयं भरें)

Roll No. (in figures) \_\_\_\_\_

अनुक्रमांक (अंकों में)

Roll No. (in words) \_\_\_\_\_

अनुक्रमांक (शब्दों में)

Enrolment No. (in figures) \_\_\_\_\_

| Time : 1 : 30 Hours

| समय : 1 : 30 घण्टे

| Maximum Marks : 75

| अधिकतम अंक : 75

Name of College \_\_\_\_\_  
कॉलेज का नाम \_\_\_\_\_Signature of Invigilator  
कक्ष निरीक्षक के हस्ताक्षर

## परीक्षार्थियों के लिए निर्देश :

1. Do not open the booklet unless you are asked to do so.
2. The booklet contains 75 questions. Examinee is required to answer first 50 questions in the OMR Answer-Sheet provided and not in the question booklet. In case Examinee attempts more than 50 Questions, **first 50 attempted questions will be evaluated. All Questions carry equal marks.**
3. Examine the Booklet and the OMR Answer-Sheet very carefully before you proceed. Faulty question booklet due to missing or duplicate pages/questions or having any other discrepancy should be immediately replaced.

(Remaining Instructions on last page)

- परीक्षार्थियों के लिए निर्देश :
- प्रश्न-पुस्तिका को तब तक न खोलें जब तक आपसे कहा न जाए।
  - प्रश्न-पुस्तिका में 75 प्रश्न हैं। परीक्षार्थी को किन्हीं 50 प्रश्नों को दी गई OMR उत्तर-पत्रक पर ही हल करना है। परीक्षार्थी द्वारा 50 से अधिक प्रश्नों को हल करने की स्थिति में, प्रथम 50 उत्तरों को ही मूल्यांकित किया जाएगा। सभी प्रश्नों के अंक समान हैं।
  - प्रश्नों के उत्तर अंकित करने से पूर्व प्रश्न-पुस्तिका तथा OMR उत्तर-पत्रक को सावधानीपूर्वक देख ले। दोषपूर्ण प्रश्न-पुस्तिका, जिसमें कुछ भाग छपने से छूट गये हो या एक से अधिक बार छप गये हों या किसी भी प्रकार की कमी हो, उसे तुरन्त बदल ले।

(शेष निर्देश अन्तिम पृष्ठ पर)

(70) The partition function of two independent (non-interacting) system is given by:

(A)  $z_{ij} = z_i + z_j$

(B)  $z_{ij} = z_i - z_j$

(C)  $z_{ij} = z_i z_j$

(D)  $z_{ij} = z_i / z_j$

71. The internal energy of an ideal gas depends only:

(A) P

(B) V

(C) T

(D) Both on P and T

72. For removing the Gibbs paradox one should multiply the expression of number of microstates by a factor of:

(A)  $\frac{1}{N!}$

(B)  $2 N!$

(C)  $\frac{1}{2N!}$

(D)  $N!$

73. A gas can approach ideal behaviour only:

(A) at low temperature & low pressure

(B) at high temperature & high pressure

(C) at high pressure and low temperature

(D) at low pressure and high temperature

74. At the most probable state of a system the entropy of the system is:

(A) minimum

(B) maximum

(C) constant

(D) None of the above

75. Planck's radiation law can be derived by using

(A) M. B. Statistics

(B) B. E. Statistics

(C) F. D. Statistics

(D) All above

65. Which of the following is an example of the second order phase transitions?
- Transformation of ferromagnetic substance into paramagnetic substance at Curie temperature.
  - Transformation of water into vapour at constant temperature and volume
  - Transformation of ice into water at  $0^{\circ}\text{C}$  and 1-atmospheric pressure
  - None of these
66. Fokker-Planck equation is:
- $\frac{\partial P}{\partial q} = -\frac{\partial}{\partial v}[M_1 P] + \frac{1}{2} \frac{\partial^2}{\partial v^2}[M_2 P]$
  - $\frac{\partial P}{\partial q} = +\frac{\partial}{\partial v}[M_1 P] + \frac{1}{2} \frac{\partial^2}{\partial v^2}[M_2 P]$
  - $\frac{\partial P}{\partial q} = -\frac{\partial}{\partial v}[M_1 P] - \frac{1}{2} \frac{\partial^2}{\partial v^2}[M_2 P]$
  - $\frac{\partial P}{\partial q} = \frac{\partial}{\partial v}[M_1 P] - \frac{1}{2} \frac{\partial^2}{\partial v^2}[M_2 P]$
- (where P - Probability function  
 $v$  - velocity  
 $q$  - time difference  
 $M_n = \frac{\langle 1 \Delta v(z) 1^2 \rangle}{\tau}$   
 $\tau$  - time interval)
67. The entropy of a system in equilibrium is:
- maximum
  - zero
  - one
  - minimum but not one
68. Consider the Fermi-Dirac distribution  $f(E)$  at room temperature where  $E$  refers to energy. If  $E_F$  is the Fermi energy, which of the following is true?
- $f(E)$  is a step function
  - $f(E_F)$  has value 1/2
  - states with  $E < E_F$  are filled completely
  - None of these
69. In a Maxwell-Boltzmann system with two states of energies  $\epsilon$  and  $2\epsilon$ , respectively and a degeneracy of 2 for each state, the partition function is:
- $2e^{-2\epsilon/kT}$
  - $2e^{-3\epsilon/kT}$
  - $e^{-\epsilon/kT} + e^{-2\epsilon/kT}$
  - $2(e^{-\epsilon/kT} + e^{-2\epsilon/kT})$

58. Viscosity is:
- (A) Transport of mass
  - (B) Transport of momentum.
  - (C) Transport of energy
  - (D) None of the above
59. 1st term in Fokker Plank equation is called:
- (A) Fluctuating Force Term
  - (B) Friction term
  - (C) Drift term
  - (D) Diffusion term
60. Landau theory of phase transition describes:
- (A) Zero order phase transition
  - (B) second order phase transition,
  - (C) first order phase transition
  - (D) all of the above
61. Which of the following is not the essential feature of Brownian motion:
- (A) The motion of each particle is completely irregular & random
  - (B) The laws of kinetic theory of gases are not applicable to Brownian motion .
  - (C) The smaller particles appears to be more agitated than the bigger particles
  - (D) The motion becomes more violent on increasing the temperature
62. According to Langavins theory of Brownian motion, the force experienced by a suspended particles are:
- (A) Frictional force & Fluctuating force .
  - (B) Gravitational force & Nuclear force
  - (C) Electromagnetic force & Nuclear force
  - (D) Nuclear force & Fluctuating force
63. Landau's theory of phase transitions is related to:
- (A) Enthalpy of a thermodynamic system
  - (B) Entropy of a thermodynamic system ,
  - (C) Free energy of a thermodynamic system
  - (D) None of these
64. The Gibb's function 'G' in thermodynamics is:
- (A)  $G=H+TS$ ,
  - (B)  $G=H-TS$
  - (C)  $G=T+HS$
  - (D)  $G=T-HS$
- (where H - Enthalpy,  
T - Temperature  
S - Entropy)

50. Which one is virial theorem:

- (A)  $\left\langle \sum q_i \frac{\partial H}{\partial q_i} \right\rangle = -\sum q_i p_i$
- (B)  $\left\langle \sum q_i \frac{\partial H}{\partial q_i} \right\rangle = -(\sum q_i p_i)$
- (C)  $\left\langle \sum q_i \frac{\partial H}{\partial q_i} \right\rangle = -\sum q_i p_i$
- (D)  $\left\langle \sum q_i \frac{\partial H}{\partial q_i} \right\rangle = -\sum q_i p_i$

51. The energy per unit dimension is:

- (A)  $\frac{3}{2} kT$
- (B)  $\frac{1}{3} kT$
- (C)  $\frac{1}{2} kT$
- (D)  $kT$

52. Which thermodynamical relations is correct among the following:

- (A)  $T = -\left(\frac{\partial E}{\partial V}\right)_{N,S}$
- (B)  $T = \left(\frac{\partial S}{\partial E}\right)_{N,V}$
- (C)  $T = \left(\frac{\partial S}{\partial E}\right)_{V,E}$
- (D)  $T = \left(\frac{\partial E}{\partial S}\right)_{N,V}$

53. The value of  $\ln n!$  will be:

- (A)  $n \ln n + n$
- (B)  $n \ln n - n$
- (C)  $n \ln n + \frac{1}{n}$
- (D)  $n \ln n - \frac{1}{n}$

54. The correct expression for cluster expansion of classical gas will be

- (A)  $\frac{N}{V} = \lim_{V \rightarrow 0} \left( \frac{Z}{V} \frac{\partial \ln Q}{\partial Z} \right) = \frac{1}{\lambda^3} \sum_{i=1}^{\infty} i! e_i z^i$
- (B)  $\frac{V}{N} = \lim_{V \rightarrow 0} \left( \frac{Z}{V} \frac{\partial \ln R}{\partial Z} \right) = \frac{1}{\lambda^3} \sum_{i=1}^{\infty} i! e_i z^i$
- (C)  $\frac{N}{V} = \lim_{V \rightarrow 0} \left( \frac{Z}{V} \frac{\partial \ln Q}{\partial Z} \right) = \frac{1}{\lambda^3} \sum_{i=1}^{\infty} i! e_i z^i$
- (D) None of these

55. Size of colloidal particle is:

- (A)  $(10^{-9}-10^{-6})m$
- (B)  $(10^{-3}-10^{-2})m$
- (C)  $(10^{-11}-10^{-1})m$
- (D)  $(10^{-10}-10^{-9})m$

56. Choose correct relation between  $\langle (\Delta x)^2 \rangle$  and time for 2D system:

- (A)  $\langle (\Delta x)^2 \rangle \sim 2Dt$
- (B)  $\langle (\Delta x)^2 \rangle \sim 3Dt$
- (C)  $\langle (\Delta x)^2 \rangle \sim 6Dt$
- (D)  $\langle (\Delta x)^2 \rangle \sim 4Dt$

57. In Brownian motion, fluctuating force comes due to:

- (A) Drag force
- (B) Collision milk watts of vessel
- (C) Activity of Brownian particle
- (D) random collision of molecules on Brownian particle

43. For an energy state  $E$  of a photon gas, the density of states is proportional to:
- $E^{1/2}$
  - $E$
  - $E^{3/2}$
  - $E^2$
44. In canonical ensemble the fractional fluctuation is proportional to:
- $N$
  - $N^2$
  - $N^{1/2}$
  - $N^{-1/2}$
- (N is the number of particles in the ensemble)
45. The relation between entropy and statistical probability is given by:
- $s = \log \Omega$
  - $s = k \ln \Omega$
  - $s = k \log \Omega^2$
  - None of the above
46. Fluctuations are thermodynamically negligible in:
- single phase system
  - Double phase system
  - Triple phase system
  - All the above
47. Langevin theory of Brownian motion is applied on a particle:
- free and only force is molecular bombardment
  - bound and attractive force due to ions
  - free and bound repulsive force due to ions
  - None of the above
48. The study of fluctuations as a function of time is important because it gives information about:
- thermal properties of system
  - mechanical properties of system
  - Statistical properties of system
  - dissipative properties of system
49. Helmholtz free energy of harmonic oscillator is:
- $A = -T \ln Q_n$
  - $A = kT \ln \left( \frac{h\nu}{kT} \right)$
  - $A = NkT \ln \left( \frac{h\nu}{kT} \right)$
  - $A = \ln \left( \frac{h\nu}{kT} \right)$

16. Partition function  $Z$ :

- (A)  $Z = 3 \times 10^6$
- (B)  $Z = 10^{10}$
- (C)  $Z = 2 \times 10^{10}$
- (D)  $Z = 2 \times 10^{11}$   
(where  $\beta = \frac{1}{kT}$ )

17. Consider the microcanonical ensemble, canonical ensemble and grand canonical ensemble. Which one physical property is same/constant in all the ensembles:

- (A) Temperature-T
- (B) Pressure-P
- (C) Volume-V
- (D) Total No. of particles N

18. From Fermi-Dirac statistics  $n_i$  is equal to:

- (A)  $\frac{g_i}{e^{\beta E_i} + 1}$
- (B)  $\frac{g_i}{e^{\beta E_i} - 1}$
- (C)  $\frac{g_i}{e^{-\beta E_i} + 1}$
- (D)  $\frac{g_i}{e^{-\beta E_i} - 1}$

19. In how many ways 18 Fermions can be distributed in 10 cell?

- (A) 10
- (B) 90
- (C) 1/2
- (D) 45.

20. Pauli's exclusion principle applies to:

- (A) Maxwell-Boltzmann statistics
- (B) Bose-Einstein statistics
- (C) Fermi-Dirac statistics
- (D) None of these

21. The value of probability of an event can not be:

- (A) zero
- (B) 1
- (C) 1/2
- (D) negative.

22. Which one of the following particles does not have a spin  $\frac{1}{2}$ ?

- (A) Proton
- (B) Neutron
- (C) Nutrino
- (D) Photon.

10. The statistical condition of equilibrium of two systems in thermal contact is:
- $T_A = T_B$
  - $S_A = S_B$
  - $\frac{\partial}{\partial E_A} \log W(A) = \frac{\partial}{\partial E_B} \log W(B)$
  - $W_A = W_B$
- (T - Temperature, S-Entropy,  
W-Thermodynamical probability)
31. The probability that in tossing a coin 10 times we get 5 heads and 5 tail, is:
- $252 \times 2^{-10}$
  - $252 \times 2^{10}$
  - $120 \times 2^{-10}$
  - $120 \times 2^{10}$
32. The volume of a cell in six dimensional phase space is:
- $\hbar^3$
  - $\hbar^3$
  - $\hbar^6$
  - $\hbar^{-6}$
- (where  $\hbar$  is the Plank Constant)
33. The probability of drawing two kings in succession from a well shuffled pack is:
- $\frac{1}{144}$
  - $\frac{1}{52}$
  - $\frac{1}{221}$
  - None of these
34. Which of the following particles obeys Maxwell-Boltzmann statistics?
- electrons
  - photons
  - protons
  - gas-molecules.
35. In a random distribution of 10 particles between two boxes with equal probability the number of micro-states (3, 7) is:
- 120
  - 5
  - $\frac{10}{21}$
  - $120 \times 10^{-10}$

28. The entropy of annihilation of N molecules of an ideal gas are:

(A)  $S = kN \log 2$

(B)  $S = Nk \log 2 - \frac{3}{2} Nk$

(C)  $S = Nk \log 2 + \frac{3}{2} Nk$

where  $k$  is Boltzmann constant  
and  $N$  is Avogadro constant

(D) van der Waals equation for entropy

of a perfect gas is:

(A)  $S = NV \log \frac{1}{V} \frac{2\pi m k T^{3/2}}{\pi} + \frac{3}{2} Nk$

(B)  $S = NV \log \frac{1}{V} \frac{2\pi m k T^{3/2}}{\pi} - \frac{3}{2} Nk$

(C)  $S = NV \log \frac{1}{V} \frac{2\pi m k T^{3/2}}{\pi} - \frac{5}{2} Nk$

(D)  $S = NV \log \frac{1}{V} \frac{2\pi m k T^{3/2}}{\pi} - \frac{7}{2} Nk$

where  $N$ - No. of molecules

V- Volume

m-mass of molecule

T-absolute temperature

k-Boltzmann constant

h-Planks constant)

28. For the mixing of two identical gases 'indistinguishable' the increase in the total entropy is given by:

(A)  $2N \log 2$

(B)  $\frac{1}{2} N \log 2$

(C)  $N \log 2$

(D)  $\frac{3}{2} N \log 2$

N-number of molecules

k-Boltzmann constant

29. According to statistical mechanics parameter  $\beta$  is:

(A)  $\frac{1}{k} \log W$

(B)  $\frac{1}{kT} \log (E)$

(C)  $\frac{1}{kE} (W)$

(D)  $\frac{1}{kE} \log (W)$

where E - The Total energy

W - The thermodynamical probability

D

13. Fermions have spin value:

- (A)  $\frac{1}{2}$ .
- (B) 1
- (C) 0
- (D) Anyone

14. If  $z$  be the partition function and  $\beta = \frac{1}{k_B T}$  then average energy of the system is given by:

- (A)  $-\frac{\partial}{\partial \beta} \ln z$
- (B)  $\frac{\partial}{\partial \beta} \ln z$
- (C)  $-\beta \frac{\partial}{\partial \beta} \left( \frac{\ln z}{\beta} \right)$
- (D)  $\beta \frac{\partial}{\partial \beta} \left( \frac{\ln z}{\beta} \right)$

15. Which statistics follow classical mechanics?

- (A) Maxwell Boltzmann Statistics.
- (B) Fermi Dirac Statistics
- (C) Bose Einstein Statistics
- (D) None

(16) Total energy of fermi gas at  $T \rightarrow 0K$

will be:

- (A)  $E_0 = \frac{2n}{5} E_F(0)$
- (B)  $E_0 = \frac{3n}{5} E_F(0)$
- (C)  $E_0 = \frac{2n}{5} \sqrt{E_F(0)}$
- (D)  $E_0 = \frac{3n}{5} \sqrt{E_F(0)}$

17. What will be the correct expression for Fermi gas at  $T \rightarrow 0K$

- (A)  $E_F(0) = \left[ \frac{n}{V} \times \frac{3}{8\pi} \frac{h^3}{g\pi m^{3/2} \sqrt{2}} \right]^{2/3}$
- (B)  $E_F(0) = \left[ \frac{n}{V} \times \frac{3}{8\pi} \frac{h^3}{g\pi m^{3/2} \sqrt{2}} \right]^{3/2}$
- (C)  $E_F(0) = \left[ \frac{n}{V} \times \frac{3}{4\pi} \frac{h^3}{g\pi m^{3/2} \sqrt{2}} \right]^{3/2}$
- (D)  $E_F(0) = \left[ \frac{n}{V} \times \frac{3}{4\pi} \frac{h^3}{g\pi m^{3/2} \sqrt{2}} \right]^{2/3}$

18. The correct expression for Bose temperature ( $T_B$ ) of an ideal base gas will be:

- (A)  $T_B = \left( \frac{n}{V} \right)^{2/3} \left( \frac{1}{2.612} \right)^{2/3} \frac{h^2}{2\pi mk}$
- (B)  $T_B = \left( \frac{n}{V} \right)^{5/2} \left( \frac{1}{2.612} \right)^{2/3} \frac{h^2}{2\pi mk}$
- (C)  $T_B = \left( \frac{n}{V} \right)^{5/2} \left( \frac{1}{2.612} \right)^{3/2} \frac{h^2}{2\pi mk}$
- (D)  $T_B = \left( \frac{n}{V} \right)^{5/2} \left( \frac{1}{2.612} \right)^{2/3} \frac{h^2}{2\pi mk}$

7. The particles obeying Maxwell-Boltzmann statistics are:

- (A) Electrons
- (B) Protons
- (C) Identical & Indistinguishable
- (D) Identical & distinguishable

8. Two particles are distributed in three energy states. According to Maxwell-Boltzmann statistics how many distributions are possible?

- (A) 1
- (B) 3
- (C) 6
- (D) 9.

9. The Bose-Einstein distribution function is:

- (A)  $\frac{n_i}{g_i} = \frac{1}{e^{(E_i - E_B)/kT} + 1}$
- (B)  $\frac{n_i}{g_i} = \frac{1}{e^{(E_i - E_B)/kT} - 1}$ .
- (C)  $\frac{n_i}{g_i} = \frac{1}{e^{(E_i - E_B)/kT} + 1}$
- (D)  $\frac{n_i}{g_i} = \frac{1}{e^{(E_i - E_B)/kT} - 1}$

10. Gibb's paradox arises due to:

- (A) Indistinguishability of classical particles
- (B) Distinguishability of classical particles
- (C) Incompleteness of quantum nature of the particles
- (D) absence of inter-particle interaction

11. Fermi Dirac (FD) statistics governs:

- (A) Fermions
- (B) Free electrons
- (C) both (A) and (B)
- (D) None of the above

12. Bosons have symmetrical wave function they do not obey:

- (A) Aufbau principle
- (B) Pauli's exclusion principle
- (C) Hund's rule of maximum multiplicity
- (D) Heisenberg's uncertainty principle

1. According to the Fermi-Dirac statistics the number of particles in a phase cell can be:
- any number
  - only two
  - only three
  - only one.
2. Which statistics will apply to deuterons and  $\alpha$ -particles?
- B.E.
  - F.D.
  - M.B.
  - None of these
3. For a single particle of mass  $m$  enclosed in a volume  $V$ , the number of accessible microstates in energy range  $E$  to  $E+\delta E$  is given by (the phase is given by):
- $\Omega(E) = \frac{2nV(2m)^{3/2} E^{1/2}}{\hbar^3} \delta E$
  - $\Omega(E) = \frac{2nV(2mE)^{3/2}}{\hbar^3} \delta E$
  - $\Omega(E) = \frac{2nV(2m)^{3/2}}{\hbar} \delta E$
  - $\Omega(E) = \frac{2nV(2mE)^{3/2}}{\hbar} \delta E$
4. In a canonical ensemble a system A of fixed volume is in contact with a large reservoir B. Then:
- A can change only in energy with B.
  - A can change only particles with B
  - A can change both energy & particles with B
  - A can change neither energy nor particles with B
5. Quantum statistics (i.e. B.E & F.D. statistics) approaches to classical statistics (i.e. Maxwell Boltzmann statistics) if the occupation index  $\left(\frac{n_i}{g_i}\right)$  is:
- $\frac{n_i}{g_i} = 1$
  - $\frac{n_i}{g_i} \ll 1$
  - $\frac{n_i}{g_i} \gg 1$
  - None of these
6. The Maxwell-Boltzmann energy distribution law in the general form is:
- $n_i = \frac{g_i}{e^{E/kT}}$
  - $n_i = g_i e^{E/kT}$
  - $n_i = g_i e^{-E/kT}$
  - $n_i = g_i e^{E/kT}$

19. During BE condensation all the

atoms fall back to:

- (A) Ground state.
  - (B) First excited state
  - (C) Highest excited state
  - (D) None of these
20. He shows BE condensation below what temperature?
- (A) 100.5 K
  - (B) 12.3 K
  - (C) 5.12 K
  - (D) 2.13 K.

21. Five bosons are distributed in two boxes. There are three cells in the first box and four cells in the second box. The thermodynamic probability of the macrostates (3, 2) is:

- (A) 100
- (B) 10
- (C) 50
- (D) 20

22. Spin of Boson is:

$$(A) \frac{1}{2}$$

$$(B) -\frac{1}{2}$$

$$(C) -\frac{3}{2}$$

$$(D) 0.$$

23. Which of the following is suitable statistics for photons?

- (A) Maxwell-Boltzmann Statistics
- (B) Fermi-Dirac Statistics
- (C) Bose-Einstein Statistics.
- (D) None of these

24. Phase space is a:

- (A) 3-dimensional space
- (B) 4-dimensional space
- (C) 5-dimensional space
- (D) 6-dimensional space.

25. In statistical mechanics Gibb's paradox is related to the:

- (A) additive property of the temperature
- (B) additive property of the energy
- (C) additive property of the momentum
- (D) additive property of the entropy.